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## Laplacian Matrices (1)

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A square matrix  $M$  of size  $n \times n$  that contains only zeros and ones, and only zeros in the diagonal, is called a *binary matrix*.

The Laplacian of a binary matrix  $M$  is another  $n \times n$  square matrix  $L$  with the following content:

- All cells  $L_{ii}$  (i.e. the diagonal of  $L$ ), are equal to the number of ones in row  $i$  of  $M$ .
- Any other cell in  $L$  contains the same value than the corresponding cell in  $M$  but with opposite sign (since  $M$  contains only 0 and 1, these  $L$  cells will contain 0 or -1 accordingly).

For example, the following binary matrix  $5 \times 5$ :

```
0 1 1 0 0
1 0 0 1 1
0 1 0 0 1
1 1 1 0 1
0 0 0 0 0
```

has as Laplacian the following Matrix:

```
2 -1 -1 0 0
-1 3 0 -1 -1
0 -1 2 0 -1
-1 -1 -1 4 -1
0 0 0 0 0
```

Write a program that reads one binary matrix and prints its Laplacian following the format shown in the examples.

### Input

Input consists of a number  $n > 0$ , the dimension of the binary matrix, followed by  $n \times n$  integers describing the matrix: all of them either 0 or 1, where all the diagonal entries are zero.

### Output

The output must contain the Laplacian transform of the input matrix.

#### Sample input 1

```
3
0 1 0
0 0 1
1 1 0
```

#### Sample output 1

```
1 -1 0
0 1 -1
-1 -1 2
```

### Sample input 2

```
4
0 1 1 0
1 0 0 1
1 1 0 1
0 1 1 0
```

### Sample input 3

```
3
0 0 0
0 0 0
0 0 0
```

### Sample output 2

```
2 -1 -1 0
-1 2 0 -1
-1 -1 3 -1
0 -1 -1 2
```

### Sample output 3

```
0 0 0
0 0 0
0 0 0
```

### Problem information

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Generation : 2024-07-10 12:23:20

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