

## Cheapest Routes

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We have collected abundant information about the local roads and accommodations in a region that we will traverse. Our plan is to go from city  $A$  to city  $B$  and we would like to spend the least possible money. For each road connecting two cities  $u$  and  $v$  we know the cost  $\omega(u, v) = \omega(v, u)$  to travel along that road (tolls, fuel, meals during the journey, ...). Every time we go from a city  $u$  to one of its neighbors  $v$  we must stop at  $v$  and spend there one night; we know the cost  $\omega'(v)$  of stopping at each city  $v$  (the cost added by  $A$  and  $B$  to our route is 0, since they are our initial and final points). All costs, of vertices and of edges, are non-negative. Thus the cost of the route

$$P = [A, v_1, \dots, v_n, B]$$

is

$$\text{cost}(P) = \omega(A, v_1) + \omega(v_1, v_2) + \dots + \omega(v_n, B) + \omega'(v_1) + \dots + \omega'(v_n).$$

Write a program in C++ which, given an undirected weighted graph with non-negative costs at the vertices and at the edges, and two vertices  $A$  and  $B$ , returns the cost of the cheapest route to go from  $A$  to  $B$ , or an indication that not such route exists.

### Input

All data in the input are non-negative integers. The input starts with two integers  $2 \leq n \leq 10000$  and  $m$ ,  $0 \leq m \leq 20n$ . After that, a sequence of non-negative integers  $\omega'(0), \dots, \omega'(n-1)$  of the weights  $\omega'(u)$  of the  $n$  vertices of the graph. Then the input contains a sequence of the  $m$  edges in the graph as triplets of the form  $\langle u, v, \omega(u, v) \rangle$ . Vertices  $u$  and  $v$  are integers in  $\{0, \dots, n-1\}$  and the weights  $\omega(u, v)$  are non-negative integers. You can assume that there are no two different edges connecting the same pair of vertices nor any edge connecting a vertex to itself. Finally, there is a sequence of pairs  $\langle A_i, B_i \rangle$ , with each  $A_i$  and  $B_i$  denoting vertices of the graph ( $0 \leq A_i, B_i < n$ ).

### Output

For each pair  $\langle A_i, B_i \rangle$  in the input sequence the program writes the cost  $\delta$  of the cheapest route between  $A_i$  and  $B_i$ . with the format  $c(A_i, B_i) = \delta$ . If no route exists between  $A_i$  and  $B_i$  the program writes  $c(A_i, B_i) = +\infty$ . The output for each case is ended with a newline (endl).

### Sample input 1

```
6 8
3 6 10 15 5 2
0 1 2 1 2 7 2 3 2
0 2 1 1 3 4 2 4 8
3 4 2 3 0 5
0 4
1 4
2 4
3 1
4 1
```

```
2 5
2 2
```

### Sample output 1

$c(0, 4) = 19$   
 $c(1, 4) = 21$   
 $c(2, 4) = 8$

$c(3, 1) = 4$   
 $c(4, 1) = 21$   
 $c(2, 5) = +\infty$   
 $c(2, 2) = 0$

### Problem information

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