

# 23

## Double auctions

18 points

### Introduction

A double auction is an economic mechanism to allocate identical goods from different vendors to multiple buyers. In a double auction, potential buyers submit their bids and potential sellers simultaneously submit their ask prices to an auctioneer. Then an auctioneer chooses some price  $p$  that clears the market: all the sellers who asked less than  $p$  sell and all buyers who bid more than  $p$  buy at this price  $p$ . As well as their direct interest, double auctions are reminiscent of Walrasian auction and have been used as a tool to study the determination of prices in ordinary markets. In this exercise we want to implement a double auction market where HP sellers will offer their ink supplies and HP customers will bid for them.

To clear the auction, the  $M^{th}$  and  $(M + 1)^{st}$  prices are computed, where  $M$  is the total number of asks. Conceptually, finding the  $M^{th}$  and  $(M + 1)^{st}$  prices is simply a matter of sorting the bids and asks in descending order (bigger to smaller), merging them in a single lists of prices, and identifying the  $M^{th}$  and  $(M + 1)^{st}$  elements in it. The prices between the  $M^{th}$  and  $(M + 1)^{st}$  bids (inclusively) represent the range of prices for which supply balances demand.

The pricing policy that we will be using is the so named  $k$ -pricing policy where  $PK$  is computed as follows:

$$PK = k * P_{(M+1)} + (1-k) * P_M$$

Where  $k$  is the so-named welfare factor and  $P_M$  and  $P_{(M+1)}$  are the  $M^{th}$  and  $(M + 1)^{st}$  prices correspondingly.

### Input

The input will start with the input of the  $k$  welfare factor, followed by the sequence of bids (ended by a -1.0) and followed by a sequence of asks (also ended by a -1.0).

```
0.5      ← this is the value of the welfare factor.
22.1
22.5
22.7
23.0
21.9
20.1
19.8
22.6
-1.0     ← this is the end of the bids, starting asks
22.1
23.6
22.2
22.4
-1.0     ← this is the end of asks
```

## Output

The program must output the final price, the asks sold sorted in ascending order (small to big) and the bids sold sorted by descending order (big to small).

```
Price: 22.55  
Asks sold: 22.1, 22.2, 22.4  
Bids sold: 23.0, 22.7, 22.6
```

## Detailed explanation

**M = 4 (number of asks)**

**Sorted bids and asks in descending order.**

**23.6**

**23.0**

**22.7**

**22.6 -> Mth price**

**22.5 -> Mth +1 price**

**22.4**

**22.2**

**22.1**

**22.1**

**20.1**

**19.8**

**K = 0.5**

**$P = (0.5 * 22.5) + ((1 - 0.5) * 22.6) = 22.55$**

**Asks below 22.55 match with bids over 22.55**

**Asks sold: 22.1, 22.2, 22.4**

**Bids sold: 23.0, 22.7, 22.6**