Implementing a Deque with a Circular Array   X12385_en

The Doble-Ended Queue (Deque) Abstract Data Type

A **deque** (*double-ended queue*) is an abstract data type (ADT) such that an instance D supports the following methods:

D.add_first(e): Add element `e` to the front of deque D.

D.add_last(e): Add element `e` to the back of deque D.

D.delete_first(): Remove and return the first element from deque D; an error occurs if the deque is empty.

D.delete_last(): Remove and return the last element from deque D; an error occurs if the deque is empty.

Additionally, the deque ADT will include accessors:

D.first(): Return a reference to the element at the front of deque D, without removing it; an error occurs if the deque is empty.

D.last(): Return a reference to the element at the back of deque D, without removing it; an error occurs if the deque is empty.

D.is_empty(): Return `True` if deque D does not contain any elements.

len(D): Return the number of elements in deque D; in Python, we implement this with the special method `__len__`.

By convention, we assume that a newly created deque is empty, and that there is no a priory bound on the capacity of the deque. Elements added to the deque can have arbitrary type.

Implementing a Deque with a Circular Array

We can implement the `deque` ADT in much the same way as the `ArrayQueue` class provided in the **public_files** section of this problem statement implements the `Queue` ADT. The same instance variables, `_data`, `_size`, and `_front`, can be used. Whenever we need to know the index of the back of the deque, or the first available slot beyond the back of the deque, we can use modular arithmetic for the computation. For example, the implementation of the `last()` method uses the index

```
back = (self._front + self._size - 1) % len(self._data)
```

The implementation of the `ArrayDeque.add_last` method is essentially the same as that for `ArrayQueue.enqueue`, including the reliance on a `_resize` utility. Likewise, the implementation of the `ArrayDeque.delete_first` method is the same as that for `ArrayQueue.dequeue`. Implementations of `add_first` and `delete_last` use similar techniques. One sublety is that a call to `add_first` may need to wrap around the beginning of the array, which can be done using modular arithmetic to circularly *decrement* the index as follows.

```
self._front = (self._front - 1) % len(self._data)
```

Pqrogramming problem

Define an `ArrayDeque` class that implements the **double-ended queue** (*deque*) ADT as sketched above. You should also modify the main program given in the public files section of the statement so that it uses the class `ArrayDeque` instead of the class `ArrayQueue`.
Hint: Define the `ArrayDeque` class as a subclass of the `ArrayQueue` class provided.

Sample input 1	Sample output 1
| ```
0
1
11
12
``` | ```
len 0
deque empty
len 0
first error: deque empty
last error: deque empty
len 0
first error: deque empty
last error: deque empty
delete first error: deque empty
delete last error: deque empty
len 0
first error: deque empty
last error: deque empty

len 0
deque empty
0 added to the back
len 1
first 0
last 0
len 1
first 0
last 0
0 deleted from the front
delete last error: deque empty
len 0
first error: deque empty
last error: deque empty

len 0
deque empty
0 added to the front
1 added to the front
2 added to the front
3 added to the front
4 added to the front
5 added to the back
6 added to the back
7 added to the back
8 added to the back
9 added to the back
resized from 136 to 216
10 added to the back
len 11
first 4
last 10
10 deleted from the back
9 deleted from the back
8 deleted from the back
7 deleted from the back
6 deleted from the back
``` |

```
len 6                                    10 added to the back
first 4                                  11 added to the back
last 5                                   len 12
4 deleted from the front                 first 5
resized from 216 to 136                  last 11
3 deleted from the front                 11 deleted from the back
2 deleted from the front                 10 deleted from the back
1 deleted from the front                 9 deleted from the back
resized from 136 to 96                   8 deleted from the back
0 deleted from the front                 7 deleted from the back
5 deleted from the front                 6 deleted from the back
delete last error: deque empty           len 6
len 0                                    first 5
first error: deque empty                 last 0
last error: deque empty                  5 deleted from the front
                                         resized from 216 to 136
                                         4 deleted from the front
len 0                                    3 deleted from the front
deque empty                              2 deleted from the front
0 added to the front                     resized from 136 to 96
1 added to the front                     1 deleted from the front
2 added to the front                     0 deleted from the front
3 added to the front                     delete first error: deque empty
4 added to the front                     delete last error: deque empty
5 added to the front                     len 0
6 added to the back                      first error: deque empty
7 added to the back                      last error: deque empty
8 added to the back
9 added to the back
resized from 136 to 216
```

Problem information

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