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**Arithmetic derivative****P86263\_en**

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Given a natural number  $n$ , its arithmetic derivative  $d(n)$  is defined as follows:

- $d(0) = d(1) = 0$ .
- If  $n$  is prime, then  $d(n) = 1$ .
- Let  $n = x \cdot y$ , with  $1 < x, y < n$ . Then  $d(n) = x \cdot d(y) + y \cdot d(x)$ .

For instance,  $d(4) = 2d(2) + 2d(2) = 2 + 2 = 4$ , and  $d(6) = 3d(2) + 2d(3) = 3 + 2 = 5$ . It can be proven that this definition is consistent. For example,  $d(12) = 4d(3) + 3d(4) = 4 + 12 = 16$ , and also  $d(12) = 6d(2) + 2d(6) = 6 + 10 = 16$ .

We say that  $f$  is a fixed point of  $d(n)$  if  $d(f) = f$ . For instance, 0 and 4 are fixed points. Given  $\ell$  and  $r$ , can you compute the number of fixed points of  $d(n)$  in  $[\ell..r]$ ?

**Input**

Input consists of several cases, each one with  $\ell$  and  $r$ , with  $0 \leq \ell \leq r \leq 10^{18}$ .

**Output**

For each case, print the number of fixed points of  $d(n)$  in  $[\ell..r]$ .

**Sample input 1**

```
0 4
1 20
4 4
5 23
9000000000000000000 10000000000000000000
```

**Sample output 1**

```
2
1
1
0
0
```

**Problem information**

Author: Salvador Roura

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