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**How many paths?****P84609\_en**

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Consider an  $n \times m$  matrix where each cell  $(i, j)$  has a number  $x_{ij}$  to indicate that you can jump down to a distance (measured as number of cells) between 1 and  $x_{ij}$ , either vertically, diagonally to the left, or diagonally to the right. If we call  $(0, 0)$  the upper left position, all the visited cells must have coordinates between 0 and  $n$  for the rows (this includes a row below the last one), and between 0 and  $m - 1$  for the columns. The goal is to start at row 0, and get exactly to row  $n$ . How many paths exist?

**Input**

Input consists of several cases, each with  $n$ ,  $m$ , and  $n$  rows with  $m$  natural numbers. Suppose that  $n$ ,  $m$  and the  $x_{ij}$  are between 1 and 100.

**Output**

For every case, print the number of paths that begin at any cell in the top row and end in any cell just below the bottom row, modulo  $10^9 + 7$ .

**Sample input 1**

```
1 1
1
1 3
1 1 1

2 3
1 1 1
1 1 1

5 1
99
99
99
99
99

3 4
3 7 6 3
1 2 4 2
5 1 2 9
```

**Sample output 1**

```
1
7
17
16
110
```

**Problem information**

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