Football corruption   P84060_en
Setzè Concurs de Programació de la UPC - Final (2018-09-19)

An infamous football club (let us call it X) wants to buy yet another competition. There are n teams, where $n = 2^m$ for some m. As usual, the tournament scheme is a complete binary tree, so X will have to win m matches to be the champion. The president of X knows, for every pair of teams i and j, the probability p_{ij} that i eliminates j. So he will bribe the football federation, and arrange the play offs so as to maximize the probability that X wins the competition. Can you compute that probability?

Input

Input consists of several cases, each one with n, followed by n lines with n probabilities each, where the j-th number of the i-th line is p_{ij}. Assume $1 \leq m \leq 3$, that $p_{ji} = 1 - p_{ij}$ for every $i \neq j$, and that the diagonal of the matrix has only -1. X is the first team.

Output

For every case, print the probability with four digits after the decimal point. The input cases have no precission issues.

Hint

The expected solution is a "reasonable" backtracking. For instance, 2000 tests with $n = 8$ should be solved in at most one second.

Sample input
```
2
-1 0.6
0.4 -1

4
 -1    1 0.5    0
  0   -1 0.7 0.8
0.5 0.3  -1 0.1
  1 0.2 0.9  -1

8
 -1 0.1 0.2 0.3 0.4 0.5 0.6 0.7
0.9  -1 0.9 0.8 0.7 0.6 0.5 0.4
0.8 0.1  -1 0.1 0.2 0.3 0.4 0.5
0.7 0.2 0.9  -1 0.5 0.6 0.7 0.8
0.6 0.3 0.8 0.5  -1 0.2 0.4 0.6
0.5 0.4 0.7 0.4 0.8  -1 0.8 0.4
0.4 0.5 0.6 0.3 0.6 0.2  -1 0.3
0.3 0.6 0.5 0.2 0.4 0.6 0.7  -1
```

Sample output
```
0.6000
0.4000
0.1100
```

Problem information

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Generation : 2024-05-03 00:33:39