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**Symmetric polynomials****P75097\_en**

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A polynomial  $p$  in three variables  $a$ ,  $b$  and  $c$  is *symmetric* if and only if  $p(a, b, c) = p(a, c, b) = p(b, a, c) = \dots$  for the six permutations of the variables.

For example,  $a + b + c$ ,  $ab + bc + ac$ ,  $3a^2b^2c^2$  and  $7abc + a^2bc + ab^2c + abc^2$  are symmetric polynomials, while  $ab + ac$  and  $a^2bc - ab^2c + abc^2$  are not.

We introduce the notation  $[a^i b^j c^k]$  with  $i \geq j \geq k$  to denote the symmetric polynomial that results from adding all the monomials of the form  $a^i b^j c^k$  for any permutation of  $a$ ,  $b$  and  $c$ , where all the resulting monomials appear with coefficient 1. For example,  $[a] = a + b + c$ ,  $[ab] = ab + bc + ca$ , and  $[a^2bc] = a^2bc + ab^2c + abc^2$ . (Note the special cases for the notation when the exponent of a variable is zero or one.)

Symmetric polynomials that do not have any variables of degree larger than one, that is,  $[a]$ ,  $[ab]$  and  $[abc]$ , are called *elementary* symmetric polynomials. The fundamental theorem of symmetric polynomials, already known to Newton, states that *any* symmetric polynomial can be expressed as the sum and product of elementary symmetric polynomials.

Here, we don't ask you to find these expressions. Instead, we ask you a much simpler task: calculate the product between a symmetric polynomial  $[a^i b^j c^k]$  and an elementary symmetric polynomial. (If you do this, you are not far away from establishing a recurrence relation and explicitly finding the expressions from the fundamental theorem.)

**Input**

Input consists of several cases, each with the product of a symmetric polynomial and an elementary symmetric polynomial. Assume  $i \geq 1$  and  $0 \leq k \leq j \leq i \leq 1000$ .

**Output**

For every product, print its result. Make sure that the terms are in lexicographical order, that is, first the term with the largest  $i$ , and in case of a tie, first the term with the largest  $j$ .

**Sample input 1**

```
[a] * [a]
[ab] * [a]
[a^2b] * [ab]
[a^3b] * [ab]
[a^3b] * [abc]
[a^1000b^700c^42] * [ab]
```

**Sample output 1**

```
[a^2] + 2[ab]
[a^2b] + 3[abc]
[a^3b^2] + 2[a^3bc] + 2[a^2b^2c]
[a^4b^2] + 2[a^4bc] + [a^3b^2c]
[a^4b^2c]
[a^1001b^701c^42] + [a^1001b^700c^43] + [a^1000b^701c^43]
```

## Problem information

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Generation: 2026-01-25T11:50:13.610Z

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