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The Virtual Learning Environment for Computer Programming

## Cooperative game

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Competitions are not in fashion anymore. What is fashionable now are cooperative games, where the participants collaborate to achieve a common goal. So, $n$ friends get inspired by the chain game, in which an array of people whisper a message $M$ in order from one extreme to the other one, trying that $M$ gets not corrupted on the way. But, to make the game more fun, some changes are made:
Let $x$ be the initial transmitter of $M$, and let $y$ be the final receiver. At each step of the game, the person $u$ that just got $M$ (or $x$, if it is the first round) must choose another person $v$ and transmit $M$ to him or her. For every pair $(u, v)$, we know the probability $p_{u v}$ that the direct transmision of the message from $u$ to $v$ is correct. That probability is independent of the round. A corrupted message never gets recovered. The game ends when $M$ reaches $y$.
Playing optimally, what is the probability that $M$ gets correctly transmitted from $x$ to $y$ ?

## Input

Input consists of several cases. Every case begins with the number of friends $n$ and the number of probabilities $p_{u v}$ that are strictly positive. Follow $m$ triplets $u, v, p_{u v}$, where $u \neq v$. Finally, we have $x$ and $y$. Assume $1 \leq n \leq 10^{4}, 0 \leq m \leq 5 n$, and that every pair of $u$ and $v$ appears at most once in the input. Friends are numbered between 0 and $n-1$.

## Output

For every case, print with five digits after the decimal point the maximum probability that the message correctly reaches $y$ from $x$. If it is impossible, tell so.

## Hint

The expected solution is based upon a fundamental graph algorithm.

| Sample input | Sample output |  |  |
| :--- | :--- | :--- | :--- |
| 6 | 8 |  | 0.00078 |
| 1 | 0 | 0.02478 |  |
| 3 | 4 | 0.49787 |  |
| 3 | 1 | 0.00335 | 1.00000 |
| 0 | 5 | 0.06737 |  |
| 0 | 2 | 0.76787 |  |
| 5 | 1 | 0.00045 |  |
| 4 | 1 | 0.93533 |  |
| 2 | 3 | 0.18315 | 0.00004 |
| 3 | 5 |  |  |
| 2 | 1 |  |  |
| 0 | 1 | 1 |  |
| 1 | 0 |  |  |
| 1 | 0 |  |  |
| 0 | 0 |  |  |
| 3 | 4 |  |  |
| 2 | 0 | 0.75008 |  |
| 0 | 2 | 0.00004 |  |
| 0 | 1 | 0.01831 |  |
| 1 | 2 | 0.00091 |  |
| 0 | 2 |  |  |

## Sample input

### 00.02478

40.49787
50.06737
20.76787
10.00045
10.93533
30.18315

1
11
0

10

4
00.75008
20.00004
10.01831

2

## Problem information

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