
Swapping parentheses**P37366_en**Cinquè Concurs de Programació de la UPC - Final (2007-10-03)

Let \mathcal{P}_n be the set of words with exactly n opening parentheses and n closing parentheses, such that every $'\)'$ matches a $'($ '. For instance,

$$\mathcal{P}_3 = \{ "((()))" , "(()())" , "(()())" , "()(())" , "()()()" \} .$$

Consider the following experiment: Choose one word w from \mathcal{P}_n at random. Then, pick one $'($ ' and one $'\)'$ of w , independently at random, and swap them. What is the probability that the result is also a word in \mathcal{P}_n ?

For example, let $n = 3$. If we choose $w = "((()))"$, then there are exactly four swaps that produce a word in \mathcal{P}_3 , namely 2-4, 2-5, 3-4, 3-5. The rest of swaps (1-4, 1-5, 1-6, 2-6, 3-6) are incorrect. Each of the other words in \mathcal{P}_3 has three correct swaps. Therefore, the probability for $n = 3$ is

$$\frac{1}{5} \left(\frac{4}{9} + \frac{3}{9} + \frac{3}{9} + \frac{3}{9} + \frac{3}{9} \right) = \frac{16}{45} \simeq 0.355556 .$$

Input

Input consists of several integer numbers n between 1 and 30.

Output

For every given n , print with six digits after the decimal point the probability that swapping a random $'($ ' with a random $'\)'$ of a random word in \mathcal{P}_n produces a word also in \mathcal{P}_n .

Sample input

```
1
2
3
10
30
```

Sample output

```
0.000000
0.250000
0.355556
0.585699
0.731991
```

Problem information

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