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**Toric necklaces****P26979\_en**

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A shop wants to commercialize a new kind of jewellery: toric necklaces! Given an infinite supply of  $k$  different beads, a toric necklace is built by picking  $n \cdot m$  beads and placing them on an  $n \times m$  grid. Then we join every pair of beads that are vertically adjacent with blue thread, and every pair of beads that are horizontally adjacent with red thread. Finally, we use blue thread to join the  $j$ -th bead of the first row with the  $j$ -th bead of the last row, and red thread to join the  $i$ -th bead of the first column with the  $i$ -th bead of the last column.

Here, we consider two toric necklaces equivalent if one can be obtained from the other by horizontal and/or vertical rotations. In other words, two necklaces defined by the matrices  $A[0 \dots n - 1, 0 \dots m - 1]$  and  $B[0 \dots n - 1, 0 \dots m - 1]$  are equivalent if there exist  $x$  and  $y$  such that  $A[i, j] = B[(i + x) \bmod n, (j + y) \bmod m]$  for every  $i$  and  $j$ .

Given  $n$ ,  $m$  and  $k$ , can you compute the number of different toric necklaces?

**Input**

Input consists of several different cases, each one with  $n$ ,  $m$  and  $k$ , all between 1 and  $10^6$ .

**Output**

For every case, print the number of  $n \times m$  toric necklaces that can be built with beads of  $k$  different kinds, modulo  $10^9 + 7$ .

**Sample input 1**

```
1 2 2
1 2 3
2 2 2
2 3 3
3 5 1
4 6 2
1 1 500
10 20 30
720680 33199 792347
1000000 1000000 1000000
```

**Sample output 1**

```
3
6
7
130
1
699600
500
798528669
229776682
320081768
```

**Problem information**

Author: Lander Ramos

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