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## Extended Fibonacci numbers

P25832\_en

Catorzè Concurs de Programació de la UPC - Final (2016-09-21)

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The well known Fibonacci numbers are defined recursively as follows:  $F_0 = 0$ ,  $F_1 = 1$ ,  $F_i = F_{i-1} + F_{i-2}$  for  $i \geq 2$ . The first Fibonacci numbers are 0, 1, 1, 2, 3, 5, 8, 13, 21, ...

Let us generalize the Fibonacci numbers. For every pair of natural numbers  $a$  and  $b$ , define the sequence  $S(a, b) = [f_0, f_1, \dots]$  as  $f_0 = a$ ,  $f_1 = b$ ,  $f_i = f_{i-1} + f_{i-2}$  for  $i \geq 2$ . Note that  $S(0, 1)$  is the traditional Fibonacci sequence.

You are given a natural number  $n$ . Please compute how many pairs  $(a, b)$  exist such that  $S(a, b)$  has a  $i \geq 3$  where  $f_i = n$ . For instance, for  $n = 2$  there are exactly three such sequences:  $S(0, 1) = [0, 1, 1, 2, \dots]$ ,  $S(1, 0) = [1, 0, 1, 1, 2, \dots]$ , and  $S(2, 0) = [2, 0, 2, 2, \dots]$ .

### Input

Input consists of several cases, each with a different natural number  $n$  between 1 and  $10^6$ .

### Output

For every  $n$ , print the number of pairs  $(a, b)$  such that  $n$  appears at a position  $i \geq 3$  in  $S(a, b)$ .

### Hint

Depending on your solution, Cassini's identity could be useful:  $F_{i-1} \cdot F_{i+1} - F_i^2 = (-1)^i$ .

### Sample input

```
2
1
3
9
10
1000
1000000
```

### Sample output

```
3
1
4
8
10
780
773883
```

### Problem information

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Generation : 2024-04-30 17:52:16

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