# Jutge.org

The Virtual Learning Environment for Computer Programming

## Systems of difference constraints

Tretzè Concurs de Programació de la UPC - Final (2015-09-16)

A system of difference constraints is a set of inequations of the kind  $x - y \le k$ , where x and y are integer variables, and k is an integer constant. Given a system of difference constraints, a *solution* is an assignment of values to variables in such a way that all inequations hold.

For instance, the system of difference constraints  $\{x_1 - x_2 \le 4, x_2 - x_3 \le -1, x_3 - x_1 \le -2\}$  has, among other solutions,  $x_1 = 4$ ,  $x_2 = 0$  and  $x_3 = 2$ .

Write a program that, given a system of difference constraints with *n* variables  $x_1, \ldots, x_n$  and *m* inequations among them, tells if there is some solution or not.

#### Input

Input consists of several cases. Every case begins with *n* and *m*, followed *m* triplets *i*, *j*, *k*, with  $i \neq j$ , for the inequation  $x_i - x_j \leq k$ . Assume  $1 \leq n \leq 10^3$ ,  $0 \leq m \leq 5n$ ,  $-10^5 \leq k \leq 10^5$ , and that every pair of *i* and *j* appears at most once. All given numbers are integers.

### Output

For every case, print "yes" if the system has some solution, and print "no" otherwise.

Sample input	Sample output
3 3 1 2 4 2 3 -1 3 1 -2	yes no yes
3 3 1 2 3 2 3 -2 3 1 -2	
4 6 2 4 -2 4 2 2 1 2 1 1 4 3 4 3 2 3 1 -1	

#### **Problem information**

Author : Enric Rodríguez Generation : 2024-04-30 17:14:58

© *Jutge.org*, 2006–2024. https://jutge.org