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**Induced subgraphs****P12120\_en**

Given an undirected graph  $G = (V, E)$ , any  $S \subseteq V$  induces a subgraph  $G[S] = (S, E')$ , where  $E'$  contains all edges in  $E$  that join two vertices in  $S$ . Let  $d(S)$  denote the minimum degree of the vertices in  $G[S]$ .

You are given a graph  $G$  and a size  $s$ . Which is the maximum degree  $d$  for which there exists some  $S$  with at least  $s$  vertices and such that  $d(S) \geq d$ ?

**Input**

Input consists of several cases, each with the number of vertices  $n$ , the number of edges  $m$ , and  $m$  pairs  $x$   $y$  (with  $x \neq y$ ), one for each edge of the graph, followed by  $s$ . The vertices are numbered from 0 to  $n - 1$ . Assume  $1 \leq n \leq 10^3$ ,  $0 \leq m \leq n(n - 1)/2$ , that there are no repeated edges, and  $1 \leq s \leq n$ .

**Output**

For every case, print the required answer.

**Sample input 1**

```
6 6
0 1  1 2  2 0  0 3  1 4  2 5
3

6 6
0 1  1 2  2 0  0 3  1 4  2 5
4

2 1
1 0
2

2 0
2

3 2
0 1  0 2
2
```

**Sample output 1**

```
2
1
1
0
1
```

**Problem information**

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